

Modeling Coal Matrix Shrinkage and Differential Swelling with CO₂ Injection for Enhanced Coalbed Methane Recovery and Carbon Sequestration Applications

Topical Report

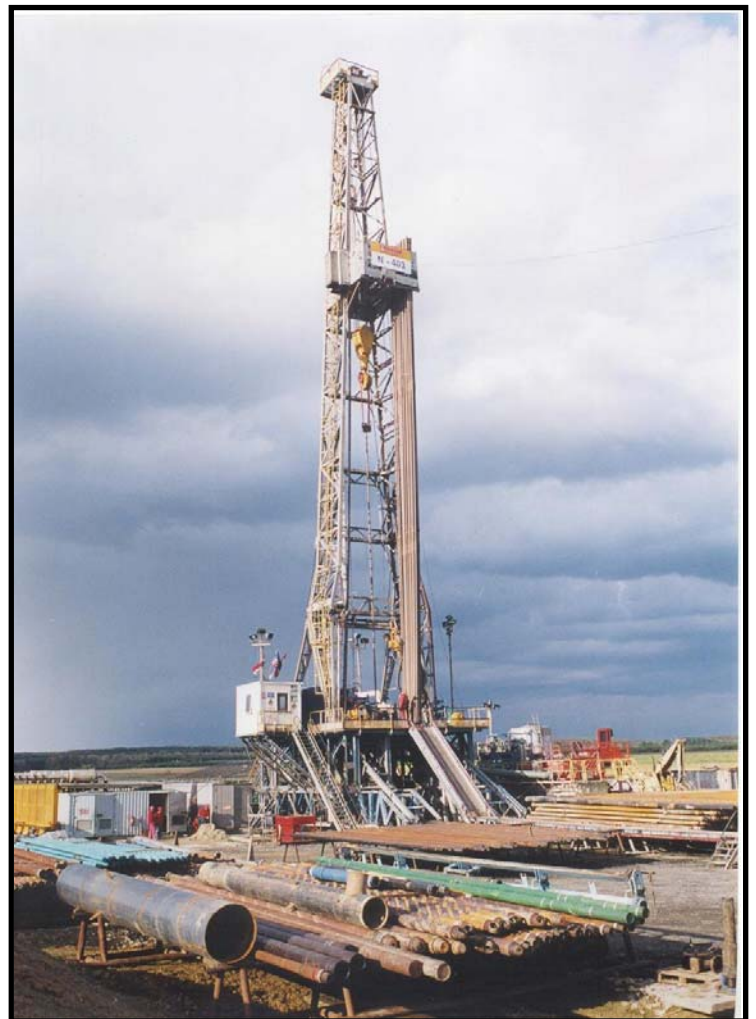
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Abstract

Matrix shrinkage and swelling can cause profound changes in porosity and permeability of coalbed methane reservoirs during depletion or when under CO₂ injection processes, with significant implication for primary or enhanced methane recovery. Two models that are used to describe these effects are discussed. The first was developed by Advanced Resources International (ARI) and published in 1990 by Sawyer, et al. The second model was published by Palmer and Mansoori in 1996. This paper shows that the two provide equivalent results for most applications. However, their differences in formulation cause each to have relative advantages and disadvantages under certain circumstances. Specifically, the former appears superior for undersaturated coalbed methane reservoirs while the latter would be better if a case is found where matrix swelling is strongly disproportional to gas concentration. Since its presentation in 1996, the Palmer and Mansoori model has justifiably received much critical praise. However, the model developed by ARI for the *COMET* reservoir simulation program has been in use since 1990, and has significant advantages in certain settings.

A review of data published by Levine in 1996 reveals that carbon dioxide causes a greater degree of coal matrix swelling compared to methane, even when measured on a unit of concentration basis. This effect is described in this report as differential swelling. Differential swelling may have important consequences for enhanced coalbed methane and carbon sequestration projects. To handle the effects of differential swelling, an extension to the matrix shrinkage and swelling model used by the *COMET* simulator is presented and shown to replicate the data of Levine.

Preliminary field results from a carbon dioxide injection project are also presented in support of the extended model. The field evidence supports that considerable changes to coal permeability occur with CO₂ injection, with significant implication for the design, implementation and performance of enhanced coalbed methane recovery and CO₂ sequestration projects.

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1.0 Introduction

Maturation of coalbed methane (CBM) production operations in some basins and the emergence of injection schemes for enhanced coalbed methane (ECBM) and carbon sequestration of greenhouse gasses has led to renewed focus on behavior of coalbed reservoir properties under these conditions. A limited body of laboratory and field data demonstrates that coal matrix shrinkage and the resulting change in cleat or fracture system porosity can have a profound effect on reservoir permeability and thus also on production (or injection) performance.

Coal has been shown to shrink on desorption of gas and expand again upon readsorption¹. Harpalani and Schraufnager² first demonstrated the impact on permeability that shrinkage had on a coal from the United States. This provided the impetus for Advanced Resources International (ARI) to develop a matrix shrinkage and permeability model that could be included in reservoir simulation software. That shrinkage model was developed for the *COMET* simulator and was published by Sawyer, et al.³ in 1990. Since 1990, other authors^{4,5,6} have shown measured strain data, that when plotted versus pore pressure, produces a curve similar to the familiar gas sorption isotherm and can be described in terms of ϵ_L and P_L which are equivalent to the Langmuir isotherm volume and pressure parameters. In 1996 Palmer and Mansoori (P&M) published a shrinkage model that described matrix shrinkage more in terms of strain and the coal's rock mechanical properties⁷. P&M issued a revised edition of their publication in 1998⁸.

This report compares the two shrinkage models and concludes that the two models provide equivalent results for the most common CBM reservoir conditions. However, different results can be expected for reservoirs that are undersaturated or have unusual swelling behavior.

Most available laboratory data, as might be expected, represents methane (CH₄) systems. The more limited data for carbon dioxide (CO₂) systems not only shows that CO₂ adsorption causes more strain and swelling than CH₄ because it is adsorbed in higher concentration by a coal, but also suggests that CO₂ causes more swelling on a unit of concentration basis. That is, 600 SCF/ton of CO₂ causes more swelling than 600 SCF/ton of CH₄. This differential swelling behavior would have important consequences for field injection projects and the ability of industry to numerically model the process. Therefore, an extension to the ARI model is also presented that accounts for this behavior.

2.0 Theoretical Models for Matrix Shrinkage/Swelling

The model developed by ARI for use in *COMET*, as presented by Sawyer et al., for the change of coal porosity due to pore compressibility, shrinkage and swelling is

$$\text{(equ.1)} \quad \phi = \phi_i \left[1 + c_p(P-P_i) \right] - c_m (1-\phi_i) \left(\frac{\Delta P_i}{\Delta C_i} \right) (C-C_i)$$

The first series of terms on the right hand side of the equation account for pressure-dependent nature of coal porosity, while the second series of terms accounts for porosity changes due to matrix shrinkage (in primary deletion cases). Figure 1 illustrates the considerable impact these

effects can have on coal permeability, based on the permeability-porosity relationship presented later in Equ.18.

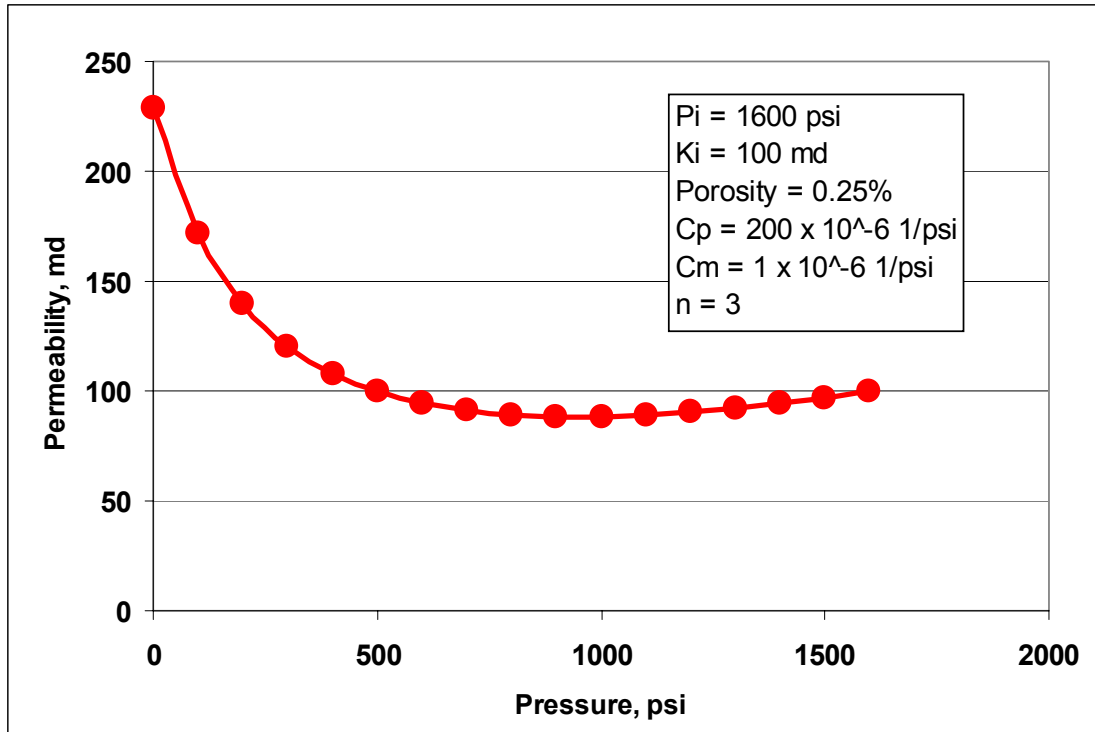


Figure 1: Effect of Pressure (and Gas Concentration) on Coal Permeability, ARI Model

The P&M model is presented as*:

$$(equ.2) \quad \frac{\phi}{\phi_i} = 1 + \frac{A_m}{\phi_i} (P - P_i) + \frac{\epsilon_L}{\phi_i} \left(\frac{K}{M} - 1 \right) \left(\frac{\beta P}{1 + \beta P} - \frac{\beta P_i}{1 + \beta P_i} \right)$$

Seidle and Huitt⁴ write the following for bulk swelling if it is proportional to adsorbed gas concentration,

$$(equ. 3) \quad \epsilon_m = S_m V_L \frac{\beta P}{1 + \beta P}$$

where S_m is the matrix swelling coefficient with units of micro strain-ton / SCF and converts the Langmuir isotherm equation to provide the amount of matrix strain, which is dimensionless.

* Minor changes to the original notation have been made since some references use the same nomenclature to define different parameters. This is especially true of the parameter c_m , which is defined in this paper as $1/V_m(\Delta V_m/\Delta P)$ and has the units of psi^{-1} . Reference No. 2 uses c'_m for the same definition. Reference No. 4 uses c_m to define a matrix swelling coefficient with units of microstrain-ton/SCF. Reference Nos. 7 and 8 also use c_m and define it in terms of elastic moduli but do not name it or describe its significance.

P&M⁷ define ϵ_L as the Langmuir dimensionless volumetric strain constant. Assuming swelling is proportional to concentration,

$$(equ\ 4) \quad \epsilon_m = S_m V_L$$

and

$$(equ\ 5) \quad \beta = \frac{1}{P_L}$$

Now, multiplying Equ.2 by Φ_i , and substituting from Eqs. 4 and 5 gives

$$(equ.\ 7) \quad \phi = \phi_i + A_m(P-P_i) + S_m V_L \left(\frac{K}{M} - 1 \right) \left(\frac{(1/P_L) P}{1 + (1/P_L) P} - \frac{(1/P_L) P_i}{1 + (1/P_L) P_i} \right)$$

Rearranging,

$$(equ.8) \quad \phi = \phi_i + A_m(P-P_i) + S_m \left(\frac{K}{M} - 1 \right) \left(\frac{V_L P}{P_L + P} - \frac{V_L P_i}{P_L + P_i} \right)$$

since gas concentration , C, is calculated by

$$(equ.\ 9) \quad C = \frac{V_L P}{P_L + P}$$

then

$$(equ.\ 10) \quad \phi = \phi_i + A_m(P-P_i) + S_m \left(\frac{K}{M} - 1 \right) (C - C_i)$$

P&M also define

$$(equ\ 11) \quad A_m = \frac{1}{M} - \left[\frac{K}{M} + f-1 \right] \gamma$$

and

$$(equ\ 12) \quad c_p = \frac{1}{\phi} \frac{d\phi}{d} = \frac{1}{\phi M}$$

where grain compressibility is small and can be disregarded,

$$(equ.\ 13) \quad A_m = \frac{1}{M} = c_p \phi$$

substituting equ 13 into Equ. 10 yields

$$(equ\ 14) \quad \phi = \phi_i + c_p \phi (P-P_i) + S_m \left(\frac{K}{M} - 1 \right) (C - C_i)$$

as noted by P&M, this is very similar to the ARI model, equ. 1.

Equating Eqs. 14 and 1

$$(equ\ 15) \quad S_m \left(\frac{K}{M} - 1 \right) = -c_m (1 - \phi_i)$$

also from P&M

$$(equ\ 16) \quad \frac{K}{M} = \frac{1}{3} \left(\frac{1+v}{1-v} \right)$$

and after rearranging Equ. 3 in terms of S_m , these can be substituted into Equ. 15 to create

$$(equ\ 17) \quad \left[\frac{1}{3} \left(\frac{1+v}{1-v} \right) - 1 \right] \epsilon_m \left(\frac{P_L - P}{V_L P} \right) = -c_m (1 - \phi_i) \frac{\Delta P_i}{\Delta C_i}$$

The two sides of this equation are dimensionally equal (gas concentration $^{-1}$). Thus the difference between the two models is reduced to the idea that P&M can be described using bulk volumetric strain, multiplied by the inverse of a Langmuir strain function and a constant determined from rock mechanical properties, whereas the ARI model employs matrix element shrinkage compressibility and the inverse slope of the isotherm as measured from the initial desorption pressure. Note that these expressions would only be equivalent for saturated reservoir conditions and cases where the strain function is proportional to the isotherm function. That is, the P&M formulation will compute matrix shrinkage to occur whenever there is a pressure change, regardless of whether there is a gas concentration change or not. This would not be appropriate for undersaturated coals.

3.0 Model Comparison

An example of the equivalence of the two methods is provided by substituting the P&M input and results from their large-scale San Juan basin evaluation⁷ into the ARI model. The basic parameters are listed in Table 1.

Table 1: Input Parameters for Model Comparison

Parameters, Units	Base Case	Sensitivity Case
Φ , %	0.1	0.5
E, psi	4.45E-05	1.24E-05
ν	0.39	-
M/E	2.0	-
K/M	0.76	-
γ , psi^{-1}	0	-
$\beta = 1/P_1$, psi^{-1}	0.0016	-
V_L , SCF/T (assumed)	600	-
P_i , psi	1100	-
ϵ_L/β	8	-

Note: $c_p = 1/2E \Phi$

For this case, $\Phi_i = 0.001$, $E = 445,000$ psi and $P = 0.0$ psi (full depletion), the P&M model determines a change in porosity from 0.001 to 0.001724. For expressing change in permeability as a function of porosity, both models use

$$\text{(equ 18)} \quad \frac{k}{k_i} = \left(\frac{\phi}{\phi_i}\right)^3$$

COMET software allows the value of the exponent to be selected by the user. This feature may be useful for particularly sensitive coals where an exponent higher than the normal default value of 3 may be necessary, as is apparently the case in some Australian coals (Xavier Choi, CSIRO Australia, personal comm.)

Although the ratio of the porosity change is 1.7, due to the exponent in Equ. 18, the ratio of the permeability change by the P&M model is 5.12. Final permeability is more than five times greater than at initial conditions. The results of P&M's San Juan evaluation is summarized in their Figure 1 and is also reproduced here as Figure 2. Note that the permeability ratio of 5.12 represents the low-pressure endpoint of the appropriate curve in Figure 2.

This set of parameters is used to determine the value of matrix shrinkage compressibility, c_m , equal to $1.784E-06$ psi^{-1} , which creates equivalence between the two models*. Results of the two models are then compared over a range of parameters for initial porosity, Young's modulus and pressure. Again, the P&M results are shown in Figure 2. Figure 3 shows that the comparable results from the ARI model are essentially identical.

In 1997, Mavor and Vaughn⁹ described modeling increasing permeability in Valencia Canyon CBM wells in the San Juan Basin. They used the P&M model to calculate lookup tables of changing porosity and permeability that were then inserted into a reservoir simulator. They remarked that no prior reservoir model explained the behavior they observed. However, as one can conclude from the previous paragraph, the ARI information published in 1990 could have been used to obtain essentially the same result.

* A value of $c_m = 1.784E-06$ psi^{-1} compares favorably with the range of laboratory measurements of c_m , as summarized in Ref. No. 4.

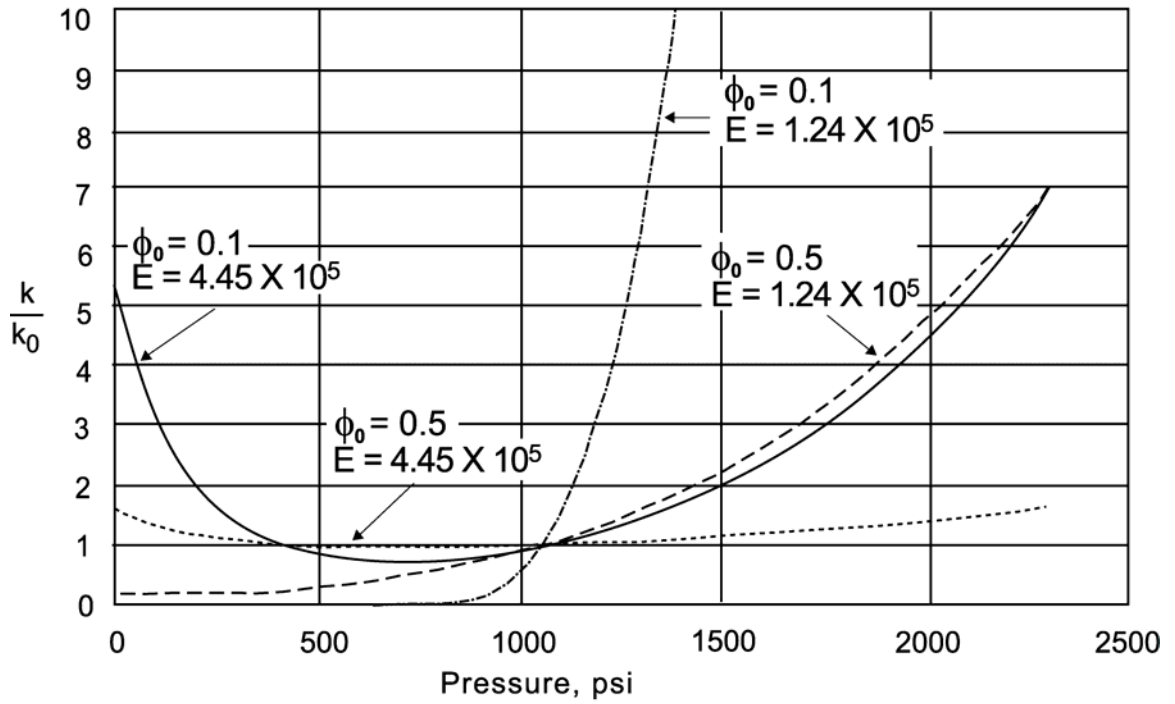


Figure 2: Effect of Pore Pressure on Coal Permeability, P&M Model (reproduced from reference 8)

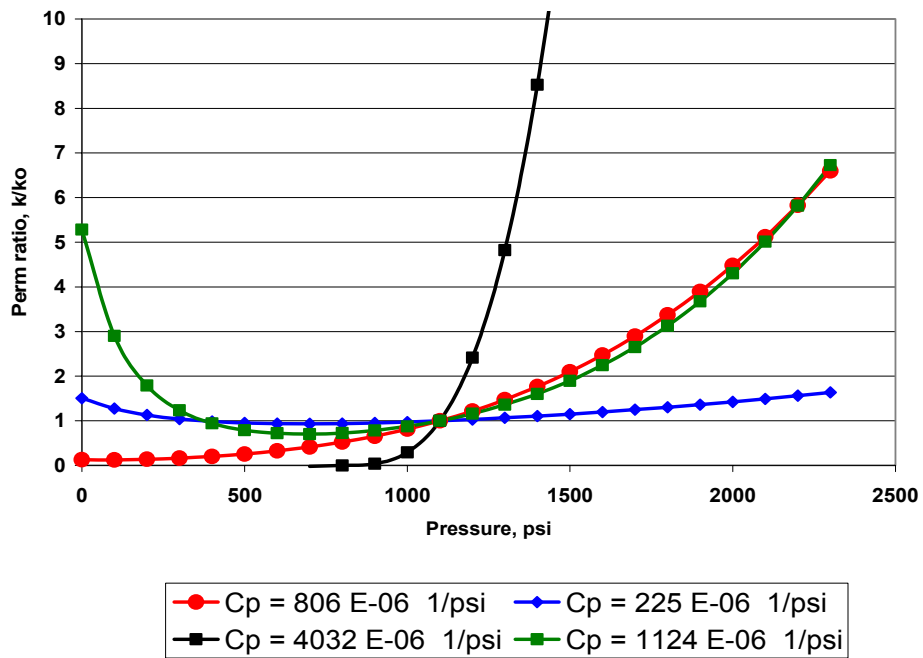


Figure 3: Comparison of ARI and P&M Model Results

4.0 Undersaturated Coals Case

The previous example shows that the two models are equivalent for coals that are initially fully saturated with methane and the degree of swelling is directly proportional to methane concentration as defined by the isotherm. However, results appear to diverge if the coals are undersaturated. P&M uses rock mechanical properties and a continuous Langmuir-type strain vs. pressure relationship. Therefore, if reservoir pressure is reduced, matrix shrinkage is calculated to occur, regardless of gas concentration changes. As pressure is reduced in an undersaturated reservoir pore compressibility effects act to reduce porosity and permeability, but no shrinkage will occur until gas desorbs and matrix gas concentration is reduced.

The ARI model directly employs the change in gas concentration to calculate shrinkage. If there is no change in concentration, as in early dewatering of an undersaturated reservoir, the model correctly calculates that there is no matrix shrinkage.

Consider again the previous example, but with the data modified to describe an undersaturated reservoir, as in Table 2. Initial pressure is 1100 psi, but saturation pressure is 800 psi.

Table 2: Additional Input Parameters For Model Comparison (Undersaturated Reservoir)

Parameter, Units	Value
P, psi	800
C _i , SCF/T	336.8

For this reservoir at 800 psi, the P&M model determines a porosity of 0.000897 (Figure 4). Overall, porosity is reduced from the original value of 0.001 due to pore volume compressibility, but approximately two-thirds of the reduction has been incorrectly offset by shrinkage. The resulting final permeability would be 72 percent of the original.

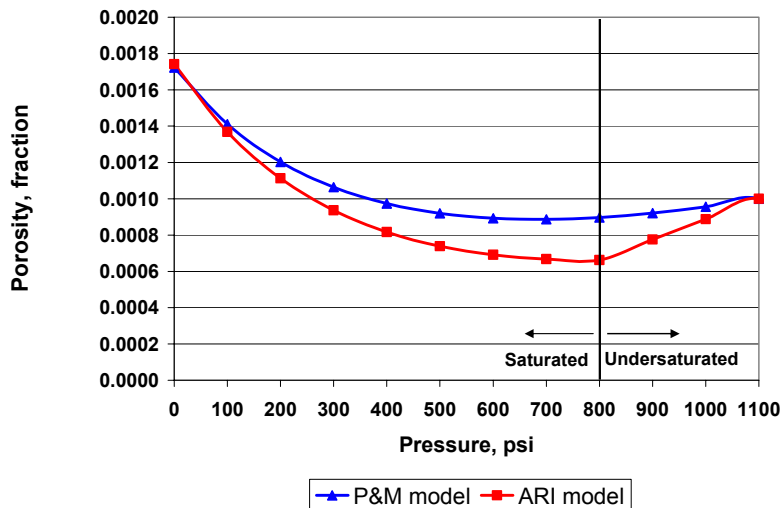


Figure 4: Variation in Coal Porosity with Pressure in an Undersaturated Reservoir

Applying these same parameters to the ARI model at 800 psi yields a final porosity of 0.000663 and a corresponding permeability only 29 percent of the original. All of the porosity change is due to pore volume compressibility. No matrix shrinkage has occurred since no gas has yet been desorbed. This result is consistent with work published by Gray¹. At pressure below 800 psi, matrix shrinkage begins to have an effect as shown by the ARI model. Eventually, at zero psi, the two models converge, both calculating the same maximum amount of shrinkage.

5.0 Swelling Not proportional to Gas Concentration Case

Laboratory studies to date^{4,5} have supported the observation that the amount of strain is approximately proportional to gas concentration. Langmuir gas concentration curves superimposed with Langmuir strain curves, as shown in Figure 5, illustrate this as a reasonable assumption, unless specific data to the contrary is known. The equivalence of the two shrinkage/swelling models, as discussed earlier, makes this assumption. However, if there is available laboratory data to show the strain function is substantially different than the gas concentration isotherm function, results of the two models will be different. If such a case is encountered, the P&M model can use the actual strain function (assuming the data can be fit to the Langmuir equation form) and would therefore be more accurate in predicting changes in porosity and permeability. The ARI model is limited to using the actual Langmuir adsorption isotherm. If the strain vs. pressure relationship does not follow the general form of the Langmuir equation, both models would be inaccurate in predicting porosity and permeability changes.

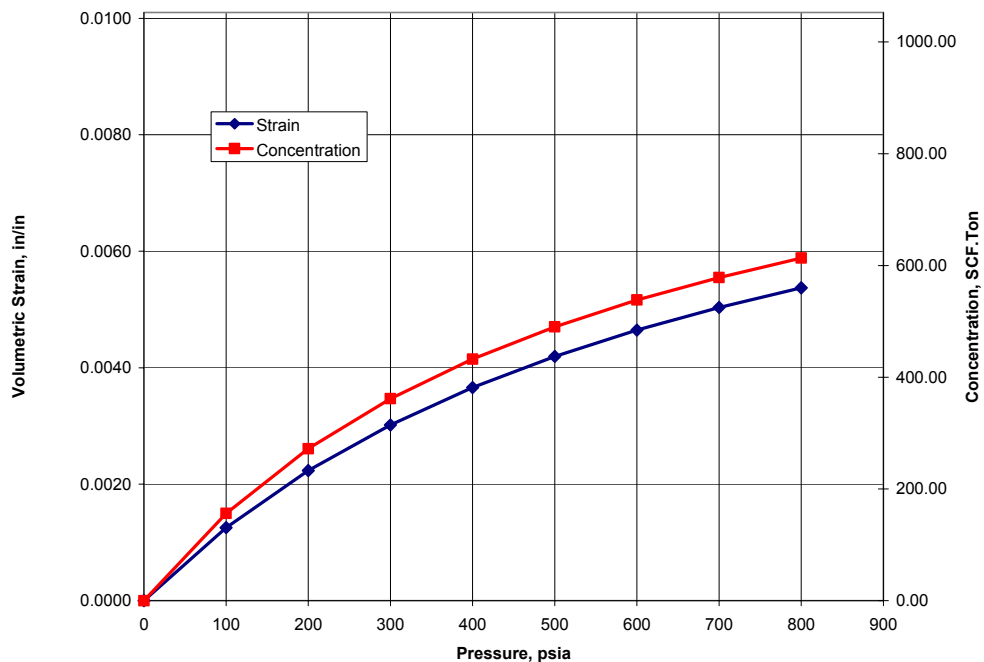


Figure 5: Pressure vs. Strain and Gas Concentration

6.0 Differential Swelling

Levine⁵ and others^{2,4,6} have shown that exposing coal to CO₂ causes differing amounts of strain or permeability change compared to similar experiments using methane or helium, which is non-adsorptive. Much of this difference is attributable to the differing sorption capacity that a coal specimen has for a particular gas. That is, the more gas adsorbed by a coal at a given pressure, the larger the effect on strain, porosity and permeability. Bustin¹⁰ has recently investigated differing adsorptive capacities for a variety of gasses.

However, review of Levine's data reveals another mechanism is also at work. Replotting his data as volumetric strain vs. concentration (Mavor, Tesseract, personal comm.), as in Figure 6, shows that, on a unit concentration basis, CO₂ causes a greater degree of strain as compared to CH₄. Porosity and permeability would then be similarly affected. This observed difference is defined here as differential swelling. The authors make no comment on the physical or chemical basis for the existence of differential swelling, which may be an appropriate topic for additional academic and laboratory research. The authors are not aware of additional data for other gasses, but believe it is reasonable to speculate that other gasses could each produce their own differential swelling effect. Such effects may cause more or less coal swelling, compared to CH₄.

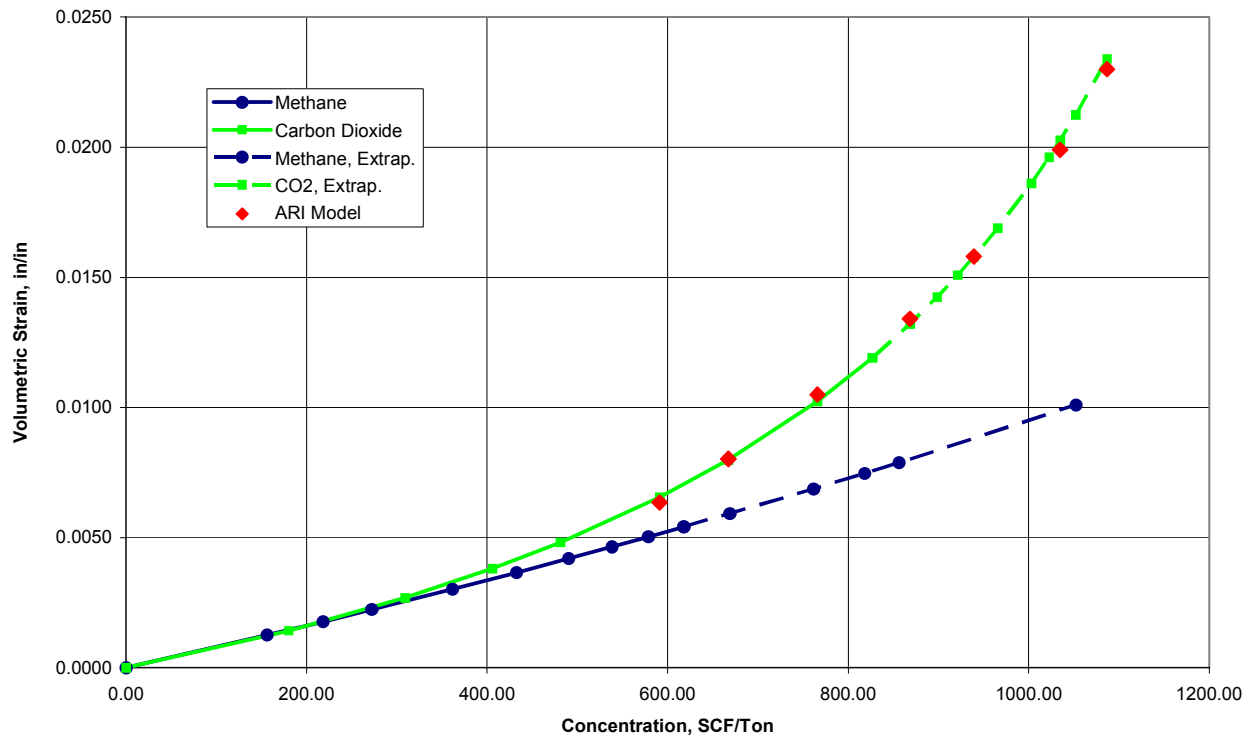


Figure 6: Strain vs. Concentration

Accounting for the impact of differential swelling in the reservoir would be an important consideration for numerical simulation of ECBM and CO₂ sequestration projects, both of which

involve injecting significant volumes of CO₂. The practical implication of differential swelling is that injection of high pressure CO₂ may cause a greater degree of permeability loss than expected simply due to changes in in-situ gas concentration.

Based on this realization, differential swelling effects have been incorporated into the *COMET* simulator. This has been accomplished by inclusion of an additional term in equation 1. This new term is a differential swelling coefficient, c_k , which can be applied to the non-methane reservoir gas concentration.

$$(equ\ 19) \quad \phi = \phi_i [1 - c_p(P-P_i)] - c_m (1-\phi_i) \left(\frac{\Delta P_i}{\Delta C_i} \right) [(C-C_i) + c_k (C_t-C)]$$

Through the addition of a differential swelling coefficient, *COMET* can effectively model the degree of matrix swelling based on the concentration of the injected gas and the amount of differential swelling the gas causes.

The differential swelling coefficient can be determined from laboratory isotherm and volumetric strain data. From Levine's data shown in Figure 6, c_k was determined to be an approximately constant value of 1.87. Use of this coefficient in Equ. 19 provides a very good replication of his CO₂ swelling data, as also shown in Figure 6.

The effect of the higher adsorptive capacity of CO₂, and differential swelling, on coal permeability are illustrated in Figure 7. This figure which is based on the same conditions for methane as presented in Figure 1, demonstrates that both the higher adsorptive capacity of CO₂ (by approximately a factor of two) and a differential swelling coefficient of 1.25, combined can reduce coal permeability by over 90% (from an initial value of 100 md at 1600 psi to less than 2.3 md). Note that the choice of differential swelling factor of 1.25 was based on independent analysis of field data. The discrepancy between this value and that from the Levine data may be related to the difference between laboratory and field-scale data.

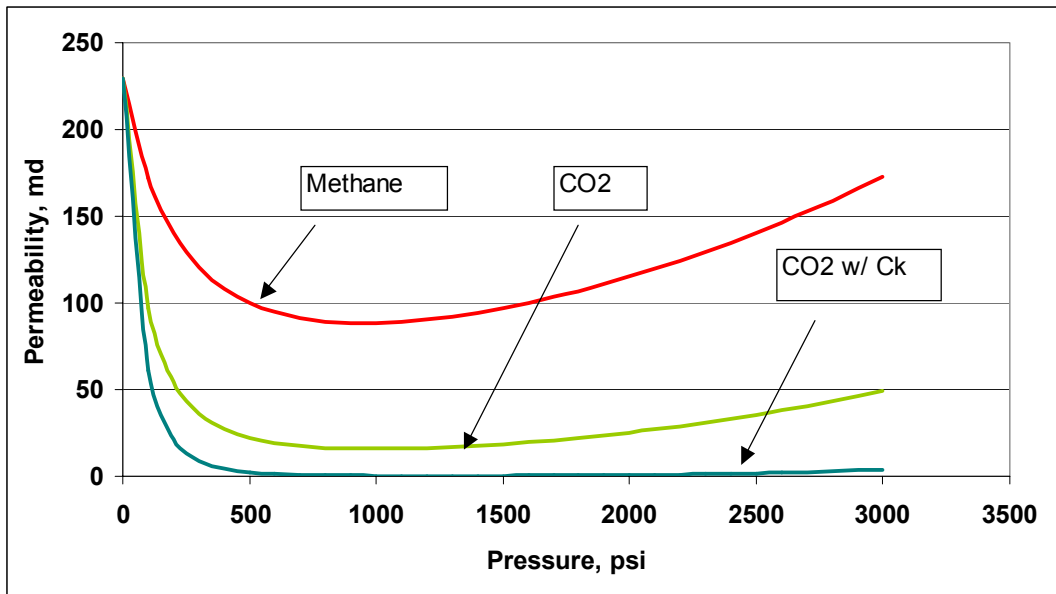


Figure 7: Effect of CO₂ and Differential Swelling on Coal Permeability

7.0 Field Evidence

Almost no field data exists for validating the laboratory findings and model predictions of coal swelling, with one notable exception. Since 1995 Burlington Resources has been injecting CO₂ into four wells in the Allison ECBM pilot in the San Juan basin. Data from those wells provides the only long-term, field-scale data to examine these phenomena.

Figure 8 presents the CO₂ injection rate and computed bottomhole pressure for one of those wells. Note that injection was performed at a relatively constant bottomhole pressure, and injection rate was permitted to vary. While injection has not been perfectly continuous, the long term injectivity trends are clear. Initially, injectivity declined significantly (from about 50,000 Mcf/mo 1.6 MMcfd at the start to a low of about 20,000 Mcf/mo (0.7 MMcfd) approximately 12 months later). Subsequent to that period of declining injectivity, injectivity began a long period of improvement, which has continued through the last available data. These trends are consistent for all four of the injection wells, and hence are believed to be real indicators of reservoir behavior.

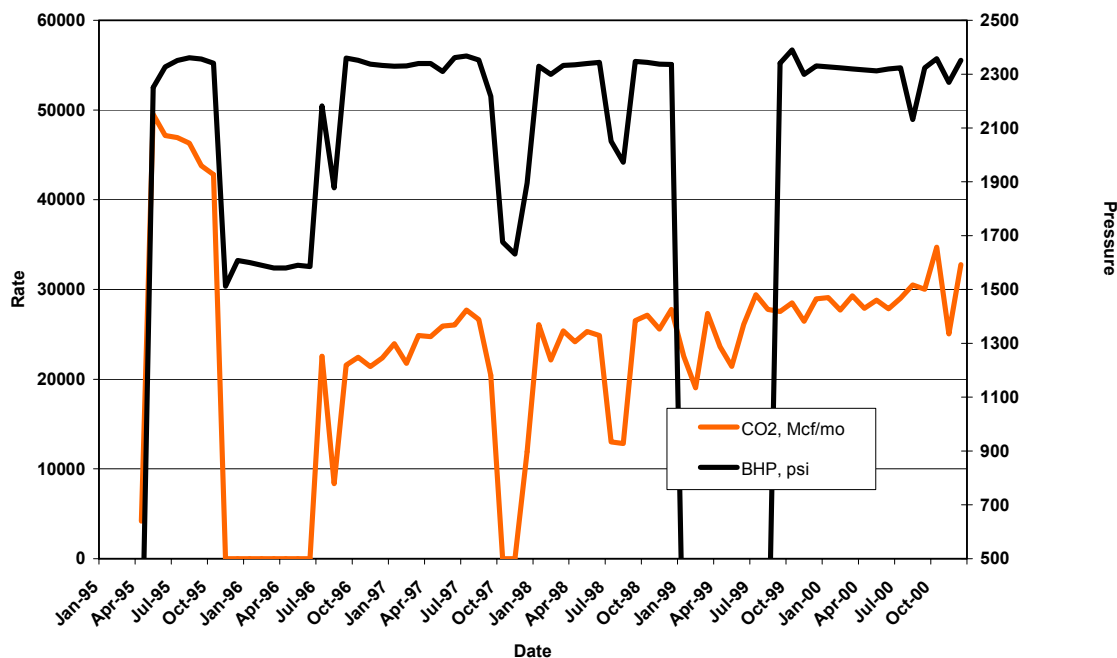


Figure 8: Injection/Pressure History for CO₂ Injection Well, Allison Unit, San Juan Basin

Pressure transient data from several producing wells in the field in the vicinity of the four injector wells had been collected in May, 2000. The results of their analysis suggested that in-situ coal permeability for the area was in the 100 – 130 md range. CO₂ contents of the produced

gas from these wells was close to their initial levels, suggesting minimal, if any, influence of injected CO₂ on these permeability results. In August, 2001, the four injector wells were shut-in, and bottomhole pressure data collected. Results of analyzing these data suggested coal permeabilities in the < 1 md range. These data provide our first field evidence into the potential magnitude of coal permeability reduction with CO₂ injection, and which are consistent with the ARI model predictions. Note that such a substantial permeability loss could not be reasonably explained without accounting for differential swelling.

Using the ARI permeability function model, the permeability history of the injector wells was rationalized. This is illustrated in Figure 9. First, coal permeability at the injection well locations declined with a reduction in pore pressure. When the injection wells were drilled and injection commenced, a rapid reduction in permeability occurred as the permeability trend shifted from the methane to the CO₂ curve. Later in injection well history, as the area under injection became further depleted and reservoir pressures declined, matrix shrinkage began to occur (as the CO₂ began desorbing from the coal), leading to a continuous and gradual improvement in injectivity. This improvement would be expected to continue with time. While somewhat subjective, this explanation is entirely consistent with field data, the results of reservoir simulation studies, and the predicted response based on the permeability function model presented in this report.

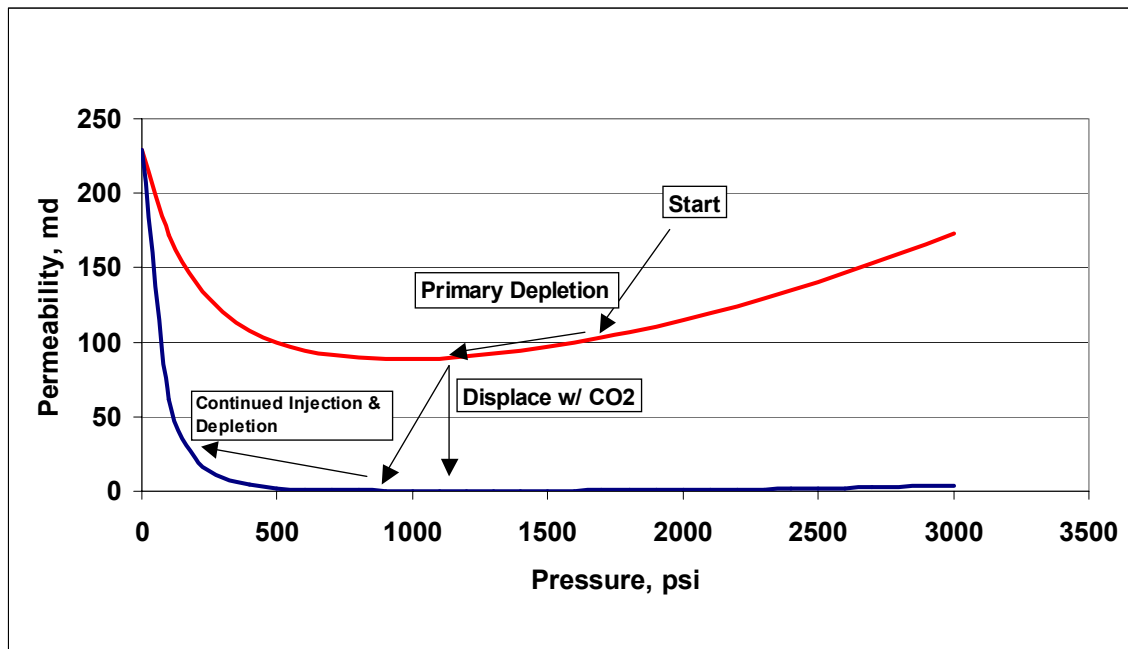


Figure 9: Permeability History for CO₂ Injection Well

8.0 Conclusions

- Matrix swelling with CO₂ injection can have a profound effect on coal permeability, and hence injectivity for CO₂ – ECBM or sequestration operations.

- For most CBM applications, the matrix shrinkage model presented by P&M in 1996 and 1998 provides results that are equivalent to the model developed by ARI for use in *COMET* in 1990.
- The ARI model appears to be superior for handling undersaturated reservoirs.
- The P&M model may be more accurate if a situation is encountered where matrix strain is weakly proportional to gas concentration. However, both models may be inaccurate where strain is not proportional to gas concentration.
- Differential swelling is a condition observed in laboratory data where CO₂ causes a different amount of volumetric strain, and by extension, a different degree of permeability change on a unit concentration basis.
- Differential swelling may also exist for other gasses, but laboratory and field studies have not yet been carried out to verify this.
- The ARI model used by *COMET* has been extended to replicate laboratory data of differential swelling. The application of this extension is demonstrated and supported by field behavior of CO₂ injection wells operating in the San Juan basin.

9.0 Nomenclature

C	=	reservoir gas concentration, dimensionless
C_i	=	initial reservoir gas concentration, dimensionless
c_k	=	differential swelling coefficient, dimensionless
c_m	=	matrix shrinkage compressibility, psi^{-1}
c_p	=	pore volume compressibility, psi^{-1}
C_t	=	total reservoir gas concentration, dimensionless
E	=	Young's modulus, psi
f	=	decimal fraction, dimensionless
K	=	bulk modulus, psi
k	=	permeability, millidarcy
k_i	=	initial permeability, millidarcy
M	=	constrained axial modulus, psi
P	=	reservoir pore pressure, psi
P_i	=	initial reservoir pore pressure, psi
P_L	=	Langmuir pressure, psi
S_m	=	matrix swelling coefficient, ton/scf
V_1	=	Langmuir volume, dimensionless
β	= $1/P_L$	inverse of Langmuir pressure, psi^{-1}
γ	=	grain compressibility, psi^{-1}
ϵ_L	=	Langmuir strain, dimensionless
ϵ_m	=	bulk strain due to matrix swelling, dimensionless
ν	=	Poisson's ratio

Φ	=	fracture system porosity, decimal fraction
Φ_i	=	initial fracture system porosity, decimal fraction

10.0 Acknowledgement

The authors thank Burlington Resources for permission to present their San Juan basin field data. We also acknowledge the helpful insights provided through personal communication with Xavier Choi of CSIRO Petroleum and Matt Mavor of Tesseract Corporation.

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